



# Trinity and St. Michael's

## Visual Calculation Policy

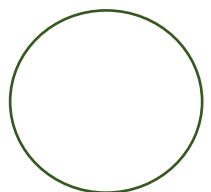
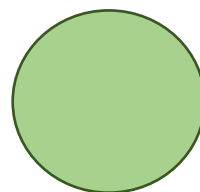
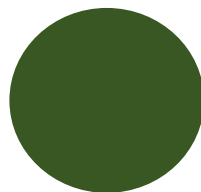
### 2021-2022

"Don't withhold good from someone who deserves it, when it is in your power to do so."  
Proverbs 3 Verse 27

Do everything in



1 Corinthians 16:13-14





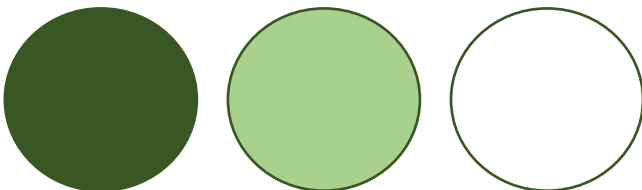
## Introduction

This document briefly outlines the methods used in the four rules of calculation. The methods are put into Key Stages. However, it is at the teacher's discretion how and when children move from one method to another. Teachers may find that children can move quickly to more abstract concepts lower down the school. Likewise, teachers might feel that going over and reminding children of more concrete and pictorial methods higher up the school is of importance.

This policy is a 'Visual Calculation Policy'. This means it is useful for reference for both parents and teachers but more information can be found in the full calculation policy.

It is worth noting that this document only includes the visual aid and explanation of how to work with addition, subtraction, multiplication and division. It does not go into detail as to how these are used within other topics (such as work with fractions, ratio etc.)

# Addition



Do everything in



1 Corinthians 16:13-14



# Addition

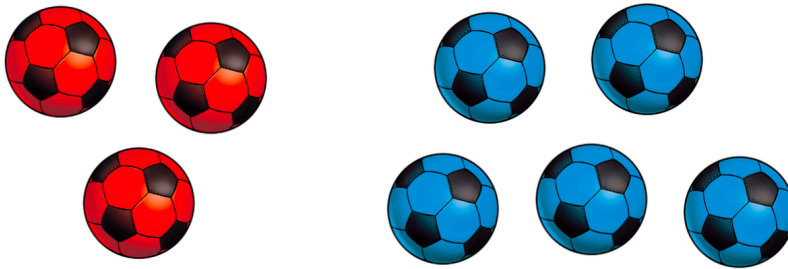
## Key Stage One

In Key Stage One things start 'Concrete'. This means we use physical objects to help the children learn how to add. This can be done with any objects but school has purchased special Maths equipment to help with this process. This equipment includes 'Numicon' and 'Base Ten'.

# A1: Objects & Pictures

1

"In the PE cupboard there were **3 red** footballs and **5 blue** footballs.  
How many footballs altogether? Answer: **8**"



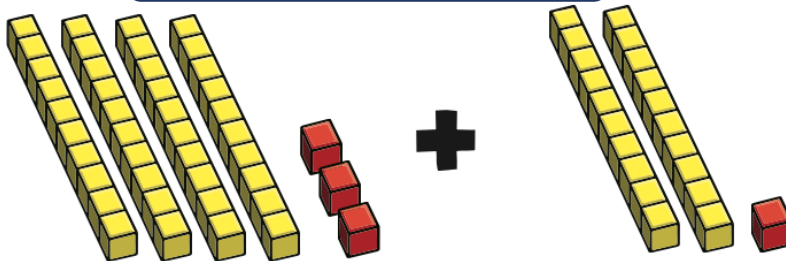
$$3 + 5 = 8$$

Numicon



$$9 + 3$$

Base Ten



$$43 + 21$$



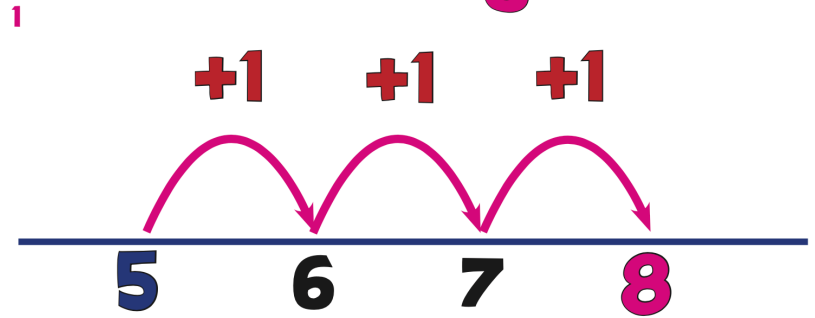
# Addition

## Key Stage One

Following this, children will start using their fingers to count on in jumps. This may well start by **counting up one** at a time. Next, children will be asked to use their ten number bonds to **get to the ten above** (the numbers that ends with a zero) and continue counting. When children develop a better understanding we may ask them to **PARTITION** a number (breaking it into tens and ones).

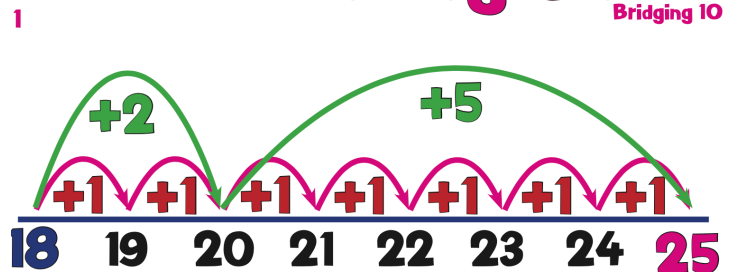
### Counting on in ones

## A2: Counting On



$$5 + 3 = 8$$

## A2b: Counting On



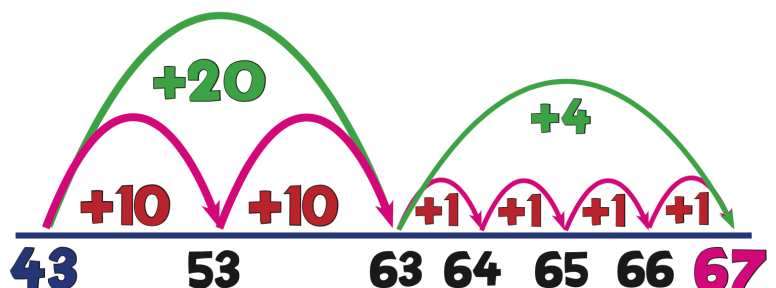
$$18 + 7 = 25$$

### Getting to the ten above

## A3: Forwards Jump

2

$$43 + 24 = 67$$



### Partitioning into TENS and ONES on Numberline

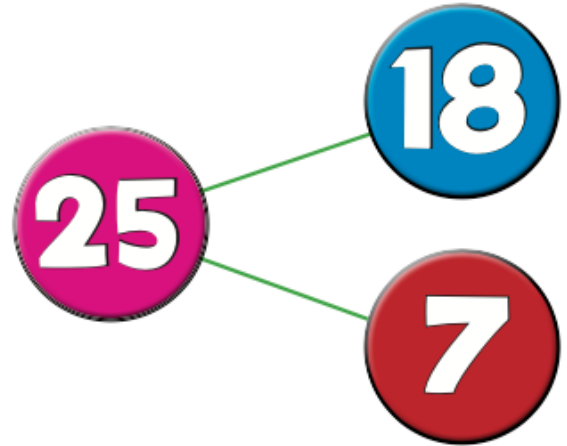


# Addition

## Key Stage One

The **Part Whole Method** allows children to visually see numbers turning into a larger number. Once we have solidified the understanding of how to partition a number this is then enforced and the children continue to look at ways we can chop numbers into smaller pieces to make them easier to deal with. This is then used through the **Part Whole Partitioning** method. Finally, towards the end of Key Stage One, some children may look at **partitioning** in a more abstract form without a numberline.

### Part Whole

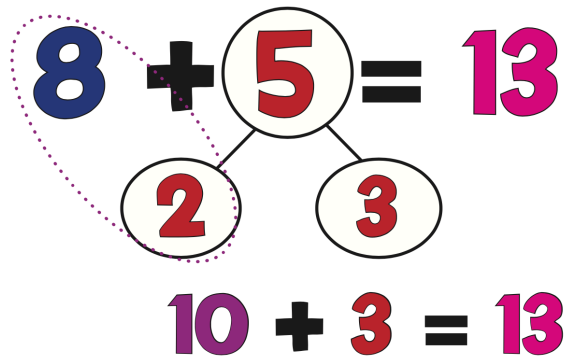


## A6: Part/Whole

1

Partitioning One Addend

### Part Whole Partitioning



### Partitioning

## A4: Partitioning

2

$$43 + 24 = 67$$

$$40 + 20 = 60$$

$$3 + 4 = 7$$

$$\underline{67}$$



# Addition

## Key Stage Two

Much like throughout Key Stage One, the key to addition in Key Stage Two is partitioning. The children start off the key stage by **partitioning** into tens and ones (eventually including hundreds). This then moves onto a more formal **numberline**.

### A4c: Partitioning

2/3

Partitioning

$$86 + 48 = 134$$

$$80 + 40 = 120$$

$$6 + 8 = 14$$

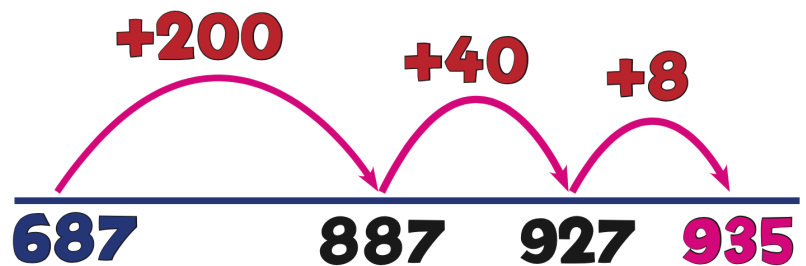

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$$134$$

### A3d: Forwards Jump

3

$$687 + 248 = 935$$



Partitioning on a  
numberline



# Addition

## Key Stage Two

By the end of Key Stage Two, all children will be comfortable with column addition. This may start with Expanded Column Addition. With this method, children are able to partition each column into ones, tens and hundreds before adding them up at the bottom. This will then lead to the more traditional column addition where numbers are carried beneath the columns.

### Expanded Column Addition

## A7d: Expanded Column Addition

3

$$\begin{array}{r}
 \begin{array}{ccc}
 100 & 10 & 1 \\
 6 & 8 & 7 \\
 + & 2 & 4 & 8 \\
 \hline
 & 1 & 5 \\
 1 & 2 & 0 \\
 8 & 0 & 0 \\
 \hline
 9 & 3 & 5
 \end{array}
 \end{array}$$

## A8e: Column Addition

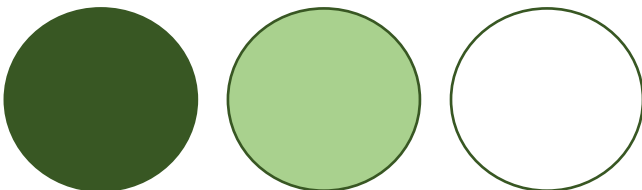
3

$$\begin{array}{r}
 \begin{array}{ccc}
 100 & 10 & 1 \\
 7 & 3 & 8 \\
 + & 5 & 2 & 4 \\
 \hline
 1 & 2 & 6 & 2 \\
 \hline
 1 & & & 1
 \end{array}
 \end{array}$$

### Column Addition



# Subtraction



Do everything in



1 Corinthians 16:13-14



# Subtraction

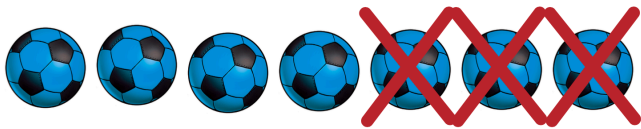
## Key Stage One

In Key Stage One things start 'Concrete'. This means we use physical objects to help the children learn how to add. This can be done with any objects but school has purchased special Maths equipment to help with this process. This equipment includes 'Numicon' and 'Base Ten'. It is important to note that the language used with subtraction may change so we are finding 'How many more' rather than 'take away'. In this case, the approach when working with concrete objects may change.

### S1: Objects & Pictures

Removing Items (Taking Away)

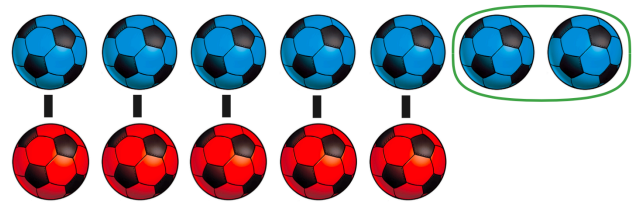
"There were 7 footballs in the PE cupboard. 3 of them were taken out. How many were left in the cupboard? Answer: 4"



$$7 - 3 = 4$$

### S1a: Objects and Pictures

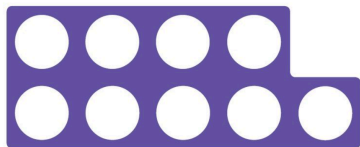
Comparing Sets



$$7 - 5 = 2$$

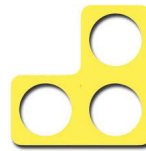
"There were 7 blue footballs and 5 red footballs? How many more blue footballs were there than red?" (What is the difference?)

### Numicon



9

-



3

### Base Ten

1

10	1
8	7
-	2
	3

2

10	1
8	7
-	2
	3

3

10	1
8	7
-	2
	3
	4

4

10	1
8	7
-	2
	3
	4

5

10	1
8	7
-	2
	3
	6
	4



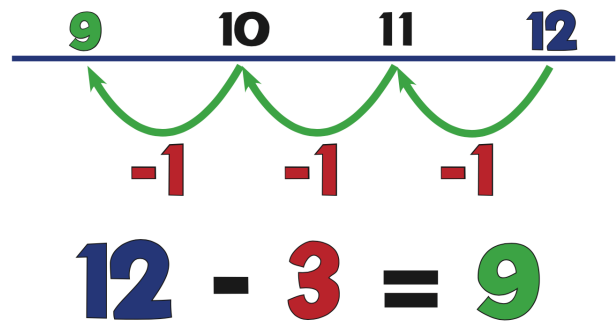
# Subtraction

## Key Stage One

In its simplest form on a numberline, children may learn about counting back in ones. Starting with the larger number on the right, the child will count back the amount that has been subtracted. Much like this concrete objects, children may learn to 'find the difference' in this instance they would write the two numbers they are subtracting from one another and count from one to the other. Both of these forms can be done with larger numbers through partitioning.

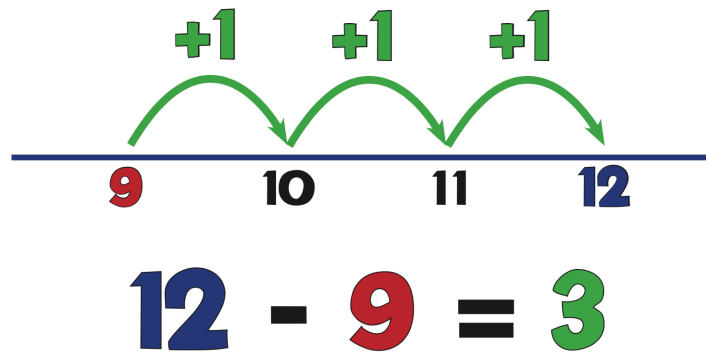
### Counting back in ones

## S2: Counting Back



"What do I get if I take 3 away from 12? Answer: 9"

## S3: Counting On

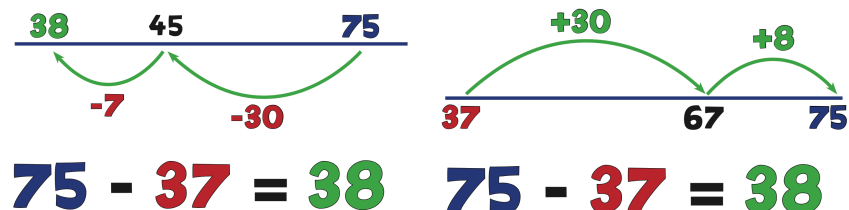


"How many more is 12 than 9? What is the difference?"

### Finding the difference in ones

### Partitioning into TENS and ONES on Numberline

## S5a: Backwards Jump S6a: 10s Jump, 1s Jump!



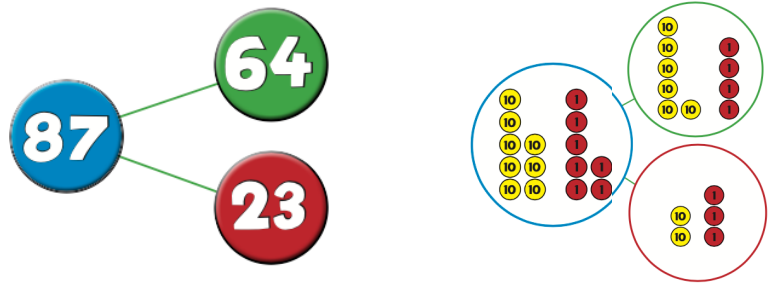


# Subtraction

## Key Stage One

The **Part Whole Method** allows children to visually see numbers turning into a larger number. Once we have solidified the understanding of how to partition a number this is then enforced and the children continue to look at ways we can chop numbers into smaller pieces to make them easier to deal with. This is then used through the **Part Whole Partitioning** method.

### Part Whole



### Part Whole Partitioning

## S8a: Part/Whole (S)

2

Partition the Subtrahend

$$75 - 37 = 38$$

$$75 - 35 = 40 \quad | \quad 40 - 2 = 38$$



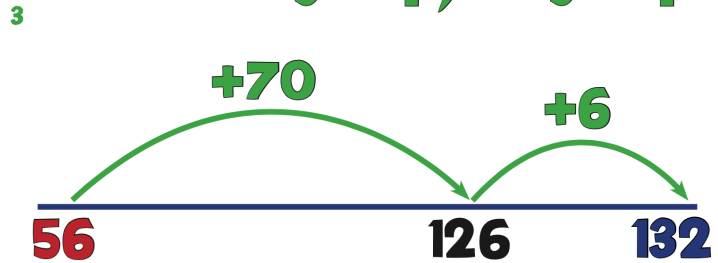
# Subtraction

## Key Stage Two

Key Stage Two begins by looking at **numberlines**. Children will start by counting on from the smaller amount to the larger. Children will then use their **numberline to make jumps**. This will take on the form of using their 10 and 100 number bonds to jump up bit by bit to the number they are subtracting from. Once children have developed that understanding of number and place value, they will look at traditional column subtraction where they will be asked to take tens and units from next door if their number is not large enough.

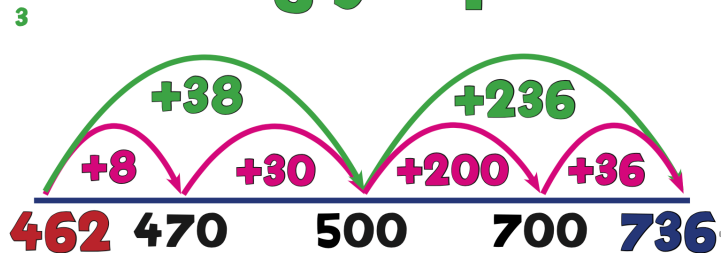
Numberline –  
Counting on

### S6c: 10s Jump, 1s Jump!



$$132 - 56 = 76$$

### S7d: Big Jump!



$$736 - 462 = 274$$

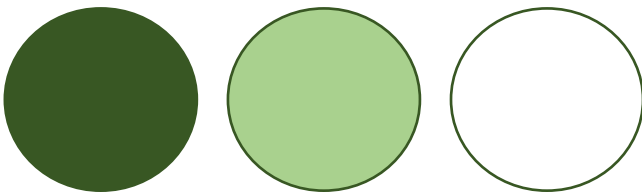
### S11a: Column Subtraction

2

$$\begin{array}{r}
 \begin{array}{c} 10 \quad 1 \\ 6 \end{array} \overline{) 75} \\
 - \quad 37 \\
 \hline
 38
 \end{array}$$

Column  
Subtraction

# Multiplication



Do everything in



1 Corinthians 16:13-14



# Multiplication

## Key Stage One

As with addition and subtraction, multiplication in Key Stage One begins with a more concrete method, using **objects and images** to see patterns and groups. This will then begin to be applied to more traditional multiplication sums as seen below. Next, children will learn to **add numbers repeatedly** – first through images and then on a numberline. **It is important to note that this is how multiplication is learnt as a method, not how times tables are learnt.**

### Concrete

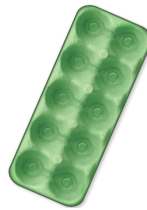
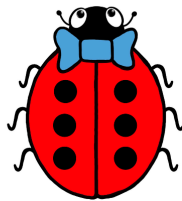
## M1a: Objects and Pictures

1



Two groups  
of three  
 $2 \times 3$

Five groups  
of four  
 $5 \times 4$



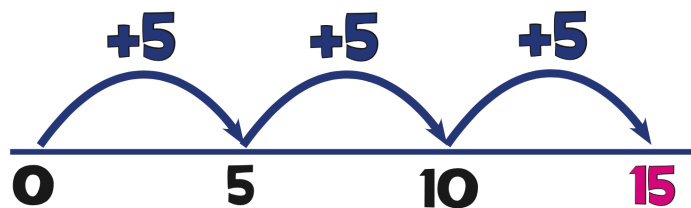
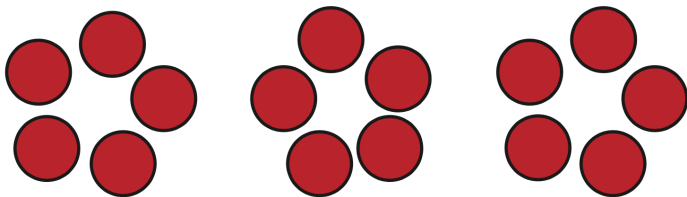
### Repeated Addition

## M2: Repeated Addition M2a: Repeated Addition

2

(Groups) 2

(Number Line)



$$5 \times 3 = 5 + 5 + 5 = 15 \quad 5 \times 3 = 5 + 5 + 5 = 15$$

"5 multiplied by 3" means "5, 3 times", which gives "3 lots of 5!"

"5 times 3" means "5, 3 times!"

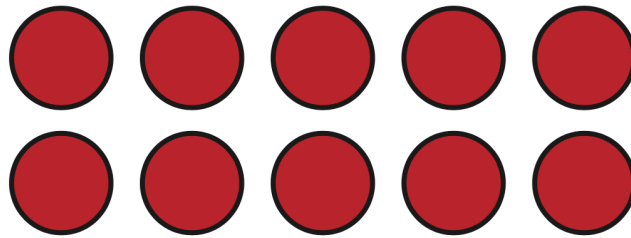


Towards the end of Key Stage One, children will begin to look at pictorial **arrays**. Using this, children are able to make groups of counters and find the answer to multiplication questions beyond the times tables they have learnt.

### Arrays

## M3: Arrays

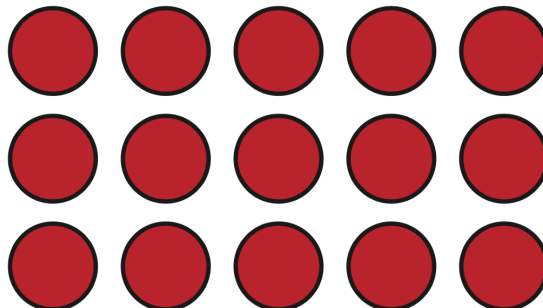
1



**“2 groups of 5 counters” or “5 groups of 2 counters” - “10 counters altogether”**

## M3: Arrays

2



$$3 \times 5 = 15 \text{ or } 5 \times 3 = 15$$





# Multiplication

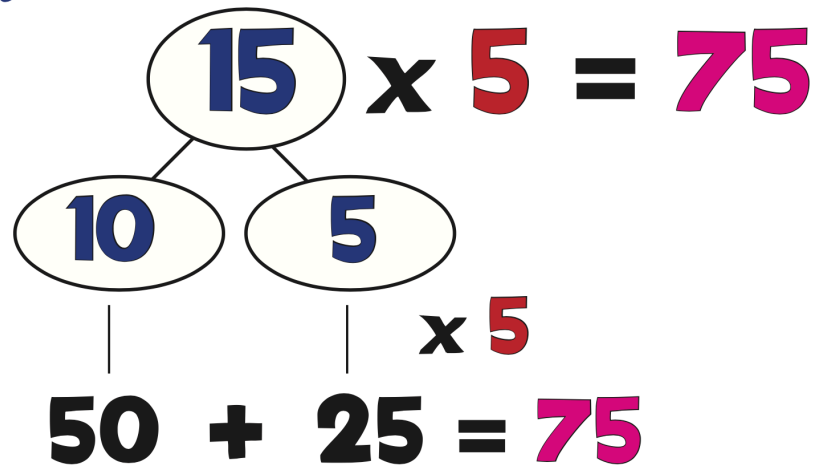
## Key Stage Two

At Key Stage One, children will need to learn their times tables up to  $12 \times 12$  by the end of Year Four. If they work with numbers larger than this, they may, to start off with, begin to **partition** this number to make it easier to deal with. This then leads on to using the **grid method** where numbers can be partitioned and then added at the end to find the answer.

## M5: Partitioning

3

### Partitioning



## M9: Grid Method

5

Long Multiplication

$$15 \times 12 = 180$$

### Grid Method

Grid method is often cited as a tricky one for parents as it is a more modern approach. The important part of this method is to first partition the numbers. Next, children must understand that, when we multiply a number that ends in a zero (e.g.  $5 \times 60$ ) we can take away the zero to answer it before putting it back in (e.g.  $5 \times 6 = 30$  so  $5 \times 60 = 300$ )

x	10	5
10	100	50
2	20	10

$$100 + 50 + 20 + 10 = 180$$



# Multiplication

## Key Stage Two

Once children have a solid understanding of how to partition larger numbers and multiply them, they will then be taught column addition. Once children start to multiply two digit numbers by two or three digit numbers they will learn long multiplication.

### M8b: Column Multiplication

4

$$\begin{array}{r}
 \begin{array}{ccc} 100 & 10 & 1 \end{array} \\
 147 \\
 \times \quad 4 \\
 \hline
 588 \\
 \hline
 1 \quad 2
 \end{array}$$

#### Column Multiplication

### M10b: Long Multiplication

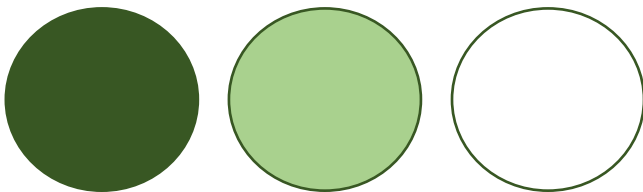
6

Column

$$\begin{array}{r}
 243 \\
 \times \quad 68 \\
 \hline
 1944 \quad (243 \times 8) \\
 + 14580 \quad (243 \times 60) \\
 \hline
 16524 \\
 \hline
 1
 \end{array}$$

#### Long Multiplication

# Division



Do everything in



1 Corinthians 16:13-14



# Division

## Key Stage One

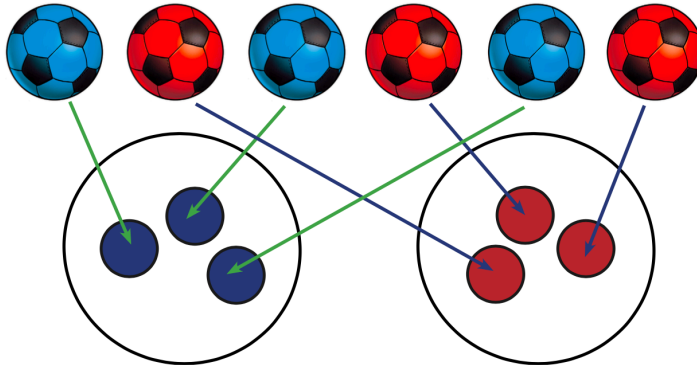
Division, as with all other areas, starts with concrete objects. Children will be asked to share these items into groups. The link with multiplication made clearer as the children go through the school. Once a concrete understanding has been achieved, children will use pictorial grouping. Children will write out circles or dots and group them by drawing around the.

### Concrete

## D1: Objects and Pictures

1

Sharing



"If I share **6 footballs** fairly into **2 bags**, how many footballs in each bag?" Answer: **3**

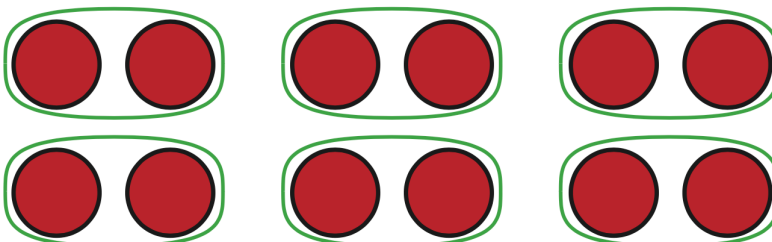
### Pictorial Grouping

## D4: Division as Grouping

2

$$12 \div 2 = 6$$

"How many groups of **2** can I fit into **12**?"  
Answer: **6**





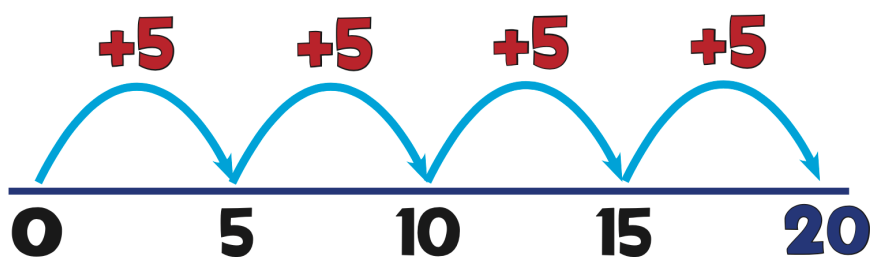
## Key Stage Two

The next step after groupings pictorially is to use a numberline. Children will start at zero and count up using the divisor (the number they are dividing by) to the dividend (the number they are dividing - see below). If children are showing great proficiency in their use of the numberline, they may well then look at dividing a larger number and using chunks to get to the dividend. E.g. if we are dividing 72 by 4 we know that  $10 \times 4$  is 40 and we would go from there to get to 72 (see below)

### Grouping on a Numberline

## D5: Grouping on a Number Line

2



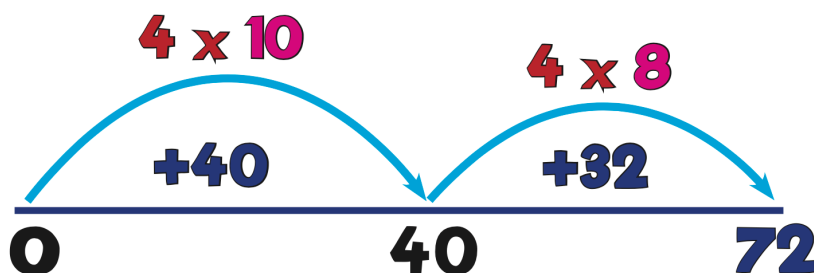
$$20 \div 5 = 4$$

"How many 5s in 20?"  
Answer: 4

### Chunking Numberline

## D7: Chunking Jump

3



$$72 \div 4 = 18$$

"How many 4s in 72?"  
Answer: 18



# Division

## Key Stage Two

When we start to divide by larger numbers, we will start with chunking. Chunking is a method that emphasises the importance of understanding number and place value. We start by taking chunks of our divisor away (for example, if we are dividing by 4, we take away chunks of  $10 \times 4$  (40) from the larger number. This way, instead of taking away four each time, we can deal with the number a lot quicker. Once we get down to a number below 40, we then deal with it like a regular division question. Finally, we add all the fours we have taken away altogether. If the number is larger, we may take away 100 of our divisor at a time (see below).

### Chunking

## D11bB: Chunking

4

$$\begin{array}{r}
 \phantom{4} \overline{) 136} \\
 \underline{- 40} \quad (4 \times 10) \\
 \phantom{4} 96 \\
 \underline{- 40} \quad (4 \times 10) \\
 \phantom{4} 56 \\
 \underline{- 40} \quad (4 \times 10) \\
 \phantom{4} 16 \\
 \underline{- 16} \quad (4 \times 4) \\
 \phantom{4} 0
 \end{array}$$

$$136 \div 4 = 34$$

### Large Chunking

## D11h: Chunking

5

$$\begin{array}{r}
 \phantom{5} \overline{) 846} \\
 \underline{- 500} \quad (5 \times 100) \\
 \phantom{5} 346 \\
 \underline{- 300} \quad (5 \times 60) \\
 \phantom{5} 46 \\
 \underline{- 45} \quad (5 \times 9) \\
 \phantom{5} 1
 \end{array}$$

Mega Chunk

$$846 \div 5 = 169r1$$



# Division

## Key Stage Two

Once we feel children have a good grasp of division being the inverse of multiplication and how we are finding how many divisors we can fit into a dividend we approach short division (otherwise known as 'the bus stop method'). Here, children see how many divisors go into each digit. Remainders are carried over from left to right. Once we deal with dividing by larger numbers (e.g. 59 as seen below), children will be asked to write this known times table next to their working out (as seen below) before answering it like short division.

### Short Division

## D10g: Short Division

5

$$5978 \div 7 = 854$$

$$\begin{array}{r}
 854 \\
 7 \overline{) 5978}
 \end{array}$$

Long Division  
(short division method).

## D12b: Long Division

6

Short Division Method

$$\begin{array}{r}
 38 \\
 59 \overline{) 2242}
 \end{array}$$

$$\begin{array}{l}
 1 \times 59 = 59 \\
 2 \times 59 = 118 \\
 3 \times 59 = 177 \\
 4 \times \dots\dots\dots
 \end{array}$$